Optimal Dual-Connectivity Traffic Offloading in Energy-Harvesting Small-Cell Networks

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Abstract—Traffic offloading through heterogenous small-cell networks (HSCNs) has been envisioned as a cost-efficient approach to accommodate the tremendous traffic growth in cellular networks. In this paper, we investigate an energy-efficient dual-connectivity (DC) enabled traffic offloading through HSCNs, in which small cells are powered in a hybrid manner including both the conventional on-grid power-supply and renewable energy harvested from environment. To achieve a flexible traffic offloading, the emerging DC-enabled traffic offloading in 3GPP specification allows each mobile user (MU) to simultaneously communicate with a macro cell and offload data through a small cell. In spite of saving the on-grid power consumption, powering traffic offloading by energy harvesting (EH) might lead to quality of service degradation, e.g., when the EH power-supply fails to support the required offloading rate. Thus, to reap the benefits of the DC-capability and the EH power-supply, we propose a joint optimization of traffic scheduling and power allocation that aims at minimizing the total on-grid power consumption of macro and small cells, while guaranteeing each served MU’s traffic requirement. We start by studying a representative case of one small cell serving a group of MUs. In spite of the non-convexity of the formulated joint optimization problem, we exploit its layered structure and propose an algorithm that efficiently computes the optimal offloading solution. We further study the scenario of multiple small cells, and investigate how the small cells select different MUs for maximizing the system-wide reward that accounts for the revenue for offloading the MUs’ traffic and the cost of total on-grid power consumption of all cells. We also propose an efficient algorithm to find the optimal MU-selection solution. Numerical results are provided to validate our proposed algorithms and show the advantage of our proposed DC-enabled traffic offloading through the EH-powered small cells.

Index Terms—Traffic offloading, small cells, energy harvesting, and dual connectivity.

I. INTRODUCTION

The past decade has witnessed an explosive growth of smart mobile devices and popularity of mobile Internet services, which have yielded a tremendous traffic burden on cellular networks. By exploiting the multi-tier structure of radio access networks (RANs), offloading mobile traffic through heterogenous small-cell networks (HSCNs) has been widely considered as a cost-efficient approach to relieve traffic congestion in macro cells. Due to bringing RANs closer to mobile users (MUs), traffic offloading through HSCNs can yield multi-fold benefits, such as enhancing throughput and improving resource utilization efficiency. To facilitate a flexible traffic offloading, the recent 3GPP specification has proposed a paradigm of small-cell dual-connectivity (DC) that enables a MU, by using two different radio interfaces, to communicate with a macro cell and simultaneously offload data through small cells [1]. With a flexible traffic scheduling between macro and small cells, the DC-enabled traffic scheduling is expected to further enhance the benefit of traffic offloading [2]–[7].

However, the dense deployment of HSCNs has yielded a significant energy consumption in cellular RANs, which has attracted lots of attentions in realizing energy-efficient HSCNs while providing guaranteed quality of service (QoS) [9]–[11]. Viewing the important role of traffic offloading, many research efforts have also been devoted to investigating energy-efficient traffic offloading through HSCNs [12]. In particular, with the recent advances in collecting and storing renewable energy from environment (e.g., via the emerging smart grids [20]), traffic offloading through small cells which are powered by energy-harvesting (EH) has been considered as a viable approach to reap the benefit of traffic offloading and to reduce the on-grid power consumption [21]–[25].
However, due to the randomness in renewable energy sources, the EH power-supply suffers from intermittency, which adversely influences the performance of traffic offloading. For instance, severe offloading outage (e.g., packet loss) due to insufficient received signal to noise and interference ratio (SINR) will occur if the small cell blindly provides a large offloading rate while suffering from a temporary valley of the EH power-supply. Several studies have been denoted to investigating how to properly exploit the intermittent EH power-supply to accommodate the MUs’ traffic. In particular, the emerging paradigm of DC, which allows the MU to simultaneously communicate with the macro and small cells, enables a flexible traffic scheduling between macro and small cells [1], [2] and thus provides an effective approach to address the intermittent EH power-supply. For instance, based on the DC, the small cell suffering from the valley of EH power-supply can slow down its offloading rate to the MU, and correspondingly, the macro cell actively increases its transmission rate to the MU in order to maintain the required QoS (e.g., throughput). Therefore, in this study, by exploiting the EH power-supply and the DC-capability, we investigate the DC-enabled traffic offloading through the EH-powered small cells. The main contributions of this paper are summarized as follows.

• We start by studying the scenario of one EH-powered small-cell access point (sAP) which offloads traffic for a group of MUs. Specifically, given the total number of served MUs, we formulate a joint optimization of the traffic scheduling and power allocation for one targeted pair of the sAP and the MU. Our formulation takes into account the offloading outage due to the sAP’s intermittent EH power-supply and aims at minimizing the total on-grid power consumption of macro and small cells, while satisfying the MU’s throughput requirement. Despite the non-convexity of the joint optimization problem, we exploit its layered structure and propose an algorithm that can efficiently compute the optimal offloading solution.

• With the optimal offloading solution for each sAP-MU pair, we further study the scenario of multiple sAPs, and investigate how the sAPs select different MUs to execute the DC-enabled traffic offloading. The formulation aims at maximizing the total network-reward that accounts for the revenue of serving the MUs’ traffic requirements and the cost of the total on-grid power consumption. Despite the nature of complicated nonlinear binary programming of the formulated optimization problem, we propose an efficient layered-algorithm to solve it and find the optimal MU-selection solution.

• We present extensive numerical results to validate our proposed algorithms (for both the single-sAP case and the multi-sAP case). Moreover, we present extensive results to show the performance advantage of our proposed DC-enabled traffic offloading through the EH-powered small cells in saving the on-grid power consumption and increasing the total network-reward.

The remainder of this paper is organized as follows. We review the related studies in Section II. We present the system model and problem formulation for the single-sAP case in Section III. An efficient algorithm to compute the optimal offloading solution is proposed in Section IV. In Section V, we further study the multi-sAP case. We present the numerical results in Section VI and finally conclude this work in Section VII.

II. RELATED LITERATURE

In this section, we firstly review the related studies about the energy-efficient traffic offloading in HSCNs but without considering the DC-capability. We then review the related studies that exploit the DC-capability for traffic offloading.

A. Studies About Energy-Efficient Traffic Offloading Through HSCNs Without DC

Without exploiting DC, there have been many studies investigating the energy-efficient traffic offloading through HSCNs, which can be in general categorized into two main streams.

• The first stream of studies focus on investigating the optimal resource allocations for energy-efficient traffic offloading (but without exploiting the EH power-supply) [12]–[19]. For instance, efficient schemes to optimize the heterogenous small cells’ on/off mode have been proposed in [12] and [13]. Efficient schemes that optimize the tradeoff between the spectrum-efficiency and energy-efficiency have been proposed in [14] and [15]. Yu et al. [16] proposed a multi-objective optimization framework that accounts for the energy-efficiency in traffic offloading. Taking into account the limited capacity of backhaul links, Yang et al. [17] proposed a refunding scheme for the small cells to accommodate the MUs offloaded from macro cells. An architecture of vertical offloading has been proposed in [18] to achieve the goal of energy-saving by actively turning off the redundant cells. In [19], an energy-efficient traffic offloading scheme that exploits device-to-device communications has been proposed.

• The second stream of studies exploit the EH power-supply for traffic offloading [21]–[25]. In [21], by exploiting the statistics information about the traffic intensity and EH power-supply, Zhang et al. proposed a scheme that jointly offloads the MUs to the EH-powered small cells and adjusts the small cells’ on/off mode. In [22], to utilize the harvested energy, Han et al. proposed a cell-size adaption scheme that actively offloads the MUs to the cells which are powered by green energy. However, aggressively offloading traffic through the EH-powered cells might lead to a severe congestion. In [23], a joint energy-aware and latency-aware scheme that offloads the MUs to the green-powered yet less congested small cells. In [24], by exploiting the advanced microgrids, Chia et al. proposed the data offloading through the microgrid-connected small cells which are powered by EH. Chang et al. [25] proposed a wireless power transfer scheme for enabling the data offloading. In addition to the above studies...
targeted for traffic offloading, there are many studies focusing on the performance analysis for the EH-powered small cells [26]–[28]. Gong et al. [26] proposed a joint optimization of the cells’ on-off states, resource blocks allocation, and renewable energy allocation to minimize the average on-grid power consumption. Yu et al. [27] developed a stochastic model to analyze the throughput and coverage performance when the small cells are powered by EH. Zheng et al. [28] investigated the optimal placement of the EH-assisted relay for offloading the cell-edge users’ traffic. Taking into account the intermittency of EH supply as well as the environmental conditions, there have been many studies investigating the transmission outage minimization [29]–[31]. For instance, Zhou et al. [29] studied the online power control policies for outage minimization in a fading wireless link with EH-powered transmitter and receiver. Li et al. [30] proposed an optimal transmission policy for minimizing the long-term transmission outage probability, when the source node is solar-powered and equipped with a finite-sized battery. In [31], based on the offline performance analysis, Isikman et al. proposed a low-complexity online transmission scheme for optimizing the outage probability in an EH block-fading communication system.

### III. System Model and Problem Formulation for One Small Cell

We firstly present the overall system model considered in this work, as shown in Figure 1. Specifically, a group of sAPs

\[ \mathcal{S} = \{1, 2, \ldots, s, \ldots, S\} \]

are underlaid to the coverage of a macro base station (mBS). The mBS is solely powered by the on-grid power-supply, and each sAP is powered by both the conventional on-grid power-supply and the EH power-supply. The sAPs and the mBS provide the DC-enabled downlink traffic offloading for a group of MUs \( \mathcal{I} = \{1, 2, \ldots, i, \ldots, I\} \). In the following Sections III and IV, we first study the case of one sAP, by specifically focusing on investigating that one sAP (together with the mBS) provides the DC-enabled traffic offloading for one MU (i.e., one sAP-MU pair). Based on the optimal offloading solution for each individual sAP-MU pair, we further study the scenario of multiple sAPs in Section V.

A. Problem Formulation for the Pair of One sAP and One MU

We start by studying the DC-enabled traffic offloading of one sAP. To present a detailed problem formulation, we focus on investigating that the sAP (together with the mBS) provides the DC-enabled traffic offloading for one MU (i.e., one sAP-MU pair), assuming that the sAP is simultaneously offloading traffic to a total number \( N_s \) MUs. Notice that we firstly consider that the value of \( N_s \) is predetermined, and the value of \( N_s \) will be further optimized for the scenario of multiple sAPs in Section V.

For the sake of clear presentation, in the following, we denote the considered sAP as sAP \( s \), and the MU as MU \( i \). MU \( i \) has a traffic requirement to achieve, which is denoted by \( R_i \). The DC enables the mBS to provide a fraction of MU \( i \)'s traffic requirement and sAP \( s \) to offload the remaining part. We consider that the mBS and sAP \( s \) use different frequency channels to serve the MUs, and thus there is no co-channel interference among the mBS’s transmission and the sAP’s transmission. We use \( p_{Bi}(s) \) to denote the mBS’s transmit-power to MU \( i \), when sAP \( s \) executes the DC-enabled offloading (notice that we include the subscript \( s \) in variable \( p_{Bi}(s) \) since the mBS’s transmit-power to MU \( i \) depends on which sAP executes the DC-enabled offloading). The downlink transmission-rate \( x_{Bi}(s) \) from the mBS to MU \( i \) can be written as:

\[
 x_{Bi}(s) = W_B \log_2 \left( 1 + \frac{p_{Bi}(s)g_{Bi}}{n_{Bi}} \right),
\]
where parameter $W_B$ denotes the mBS's downlink channel bandwidth to accommodate each MU, and $g_{Bi}$ denotes the channel power gain from the mBS to MU $i$. Parameter $n_{Bi}$ denotes the power of the background noise at MU $i$ from the mBS's transmission, e.g., $n_{Bi}$ can be expressed as $n_{Bi} = W_{Bi}n_0$, where $n_0$ is the power density of the background noise.

sAP $s$ has both the on-grid power-supply and the EH power-supply. We use $p_{si}$ to denote sAP $s$'s transmit-power to MU $i$ from its on-grid power-supply, and sAP $s$ can flexibly adjust $p_{si}$ within $[0,p_{s,\text{max}}]$ where $p_{s,\text{max}}$ denotes the maximum on-grid transmit-power). However, due to the intermittency of renewable energy sources, sAP $s$'s harvested energy, which is denote by $Q_s$, is a random variable. As mentioned before, given the total number of $N_s$ MUs served by sAP $s$, from the fairness perspective and tractability perspective, we consider that sAP $s$ equally divides $Q_s$ for all its served MUs.

As a result, the offloading rate from sAP $s$ to MU $i$ can be written as:

$$x_{si} = W_s \log_2 \left(1 + \frac{(N_sp_{si} + Q_s)g_{si}}{N_sn_{si}}\right), \tag{2}$$

where $W_s$ denotes the downlink channel bandwidth used by sAP $s$ to serve each MU, and $g_{si}$ denotes the channel power gain from sAP $s$ to MU $i$. Parameter $n_{si}$ denotes the power of the background noise at MU $i$ from the transmission of sAP $s$. In this work, to focus on our objective in investigating how to properly exploit the DC-capability to facilitate the MUs' traffic offloading and mitigate the impact of the intermittency in the EH power-supply, we adopt a relatively simple assumption on the utilization of EH power-supply (i.e., sAP $s$ equally allocates its entire EH power-supply $Q_s$ to the served $N_s$ MUs). Therefore, our result in this work provides a benchmark evaluation on exploiting the DC for traffic offloading when integrating the EH power-supply. As we present in this paper, such a design (i.e., our proposed joint traffic scheduling and power allocation) is already very challenging to solve, even under the current assumption. In particular, as an important direction for our future study, we will further consider that the sAP can flexibly schedule its EH power-supply over different time slots and allocate different amounts of the EH power-supply for different MUs, and investigate the corresponding optimal design of the DC-enabled traffic offloading.

In this work, we consider the long-term average on-grid power consumption and model $Q_s$ in each short scheduling period as an independent and uniform distribution within $[M_{s,\text{low}}, M_{s,\text{upp}}]$. The values of $M_{s,\text{low}}$ and $M_{s,\text{upp}}$ are assumed to be known based on the historical data. The uniform distribution has been used to model uncertainty in EH power-supply over short-term periods [27], [32]–[34]. For instance, in [32], based on a time-slotted structure, the authors adopted the similar uniform distribution (as well as other distributions) to model the harvested energy from solar energy. [33] used the same slotted-structure and the uniform distribution of the EH supply to investigate the network throughput maximization for sink-based wireless sensor networks. Nevertheless, it is worth noticing that the current assumption about the EH-supply is relatively ideal for some specific cases. As an important direction for our future work, we will also consider other more realistic assumptions on the EH-supply and investigate the corresponding optimal design of DC-enabled traffic offloading.

The uncertainty in $Q_s$ introduces randomness to the achievable offloading rate $x_{si}$ from sAP $s$ to MU $i$. Let $r_{si}$ denote sAP $s$'s assigned offloading rate to MU $i$. Due to the randomness in $x_{si}$, $r_{si}$ may not be satisfied, which leads to the offloading outage. To capture this outage, we introduce function $P_{\text{out}}(p_{si}, r_{si})$ to denote the probability that sAP $s$'s achievable offloading rate $x_{si}$ to MU $i$ fails to meet the assigned offloading rate $r_{si}$. Function $P_{\text{out}}(p_{si}, r_{si})$ can be written as:

$$P_{\text{out}}(p_{si}, r_{si}) = \Pr\left\{ r_{si} \geq x_{si} \right\}$$

$$= \Pr\left\{ x_{si} \geq W_s \log_2 \left(1 + \frac{(N_sp_{si} + Q_s)g_{si}}{N_sn_{si}}\right) \right\}$$

$$\leq \left\{ \begin{array}{ll}
\frac{2^{W_s r_{si}} - 1}{g_{si}} & \text{if } 2^{W_s r_{si}} - 1 \leq p_{si} \\
\frac{M_{s,\text{upp}} - M_{s,\text{low}}}{g_{si}} & \text{if } 2^{W_s r_{si}} - 1 \frac{M_{s,\text{upp}} - M_{s,\text{low}}}{N_s g_{si}} \leq p_{si} \\
0, & \text{if } 2^{W_s r_{si}} - 1 \frac{M_{s,\text{upp}} - M_{s,\text{low}}}{N_s g_{si}} < p_{si} \\
1, & \text{otherwise}
\end{array} \right. \tag{3}$$

Based on $P_{\text{out}}(p_{si}, r_{si})$, we formulate an optimization problem to minimize the total on-grid power consumption, i.e., $p_{Bi}(s) + p_{si}$ when sAP $s$ offloads traffic to MU $i$. The details are shown in the following total On-Grid Power Consumption Minimization (OGPM) problem:

$$\begin{aligned}
\text{(OGPM)} \quad \min & \quad p_{Bi}(s) + p_{si} \\
\text{Subject to:} & \quad x_{Bi}(s) + r_{si}(1 - P_{\text{out}}(p_{si}, r_{si})) = R^\text{req}_i, \\
& \quad 0 \leq p_{Bi}(s) \leq P_B^\text{max}, \\
& \quad 0 \leq p_{si} \leq p_{s,\text{max}}
\end{aligned} \tag{4}$$

Variables : $(r_{si}, p_{si})$ and $(x_{Bi}(s), p_{Bi}(s))$. \tag{5} \tag{6} \tag{7}

In Problem (OGPM), we jointly optimize the following variables: i) sAP $s$'s assigned offloading rate $r_{si}$ and the transmit-power $p_{si}$ to MU $i$, and ii) the mBS's transmission rate $x_{Bi}(s)$ and the transmit-power $p_{Bi}(s)$. Constraint (4) guarantees that MU $i$ receives a total successful throughput equal to its requirement $R^\text{req}_i$, where the term of $r_{si}(1 - P_{\text{out}}(p_{si}, r_{si}))$ denotes the successful throughput received from sAP $s$. Parameter $p_{B}^\text{max}$ denotes the mBS's maximum on-grid transmit-power for each MU, and $p_{s,\text{max}}$ denotes sAP $s$'s maximum on-grid transmit-power for each MU.

According to [35], Problem (OGPM) is a non-convex optimization problem which is difficult to solve. To address this difficulty, we exploit the layered-property of Problem (OGPM), and equivalently transform it into an equivalent form that can lead to Problem (OGPM) an efficient solution.
B. Layered Structure of Problem (OGPM)

We now consider the most general case of $P_{\text{out}}(p_{si}, r_{si}) \in [0, 1]$ (i.e., the first case in (3)). In this case, we can equivalently transform Problem (OGPM) into:

\[
\begin{align*}
\text{(OGPM)} \quad & \min p_{Bi(s)} + p_{si} \\
\quad & \text{Subject to: } W_B \log_2 \left( 1 + \frac{p_{Bi(s)} g_{Bi}}{n_{Bi}} \right) \\
\quad & \quad + \frac{M_s^{\text{upp}} + N_s p_{si} - N_s \left( 2 \frac{r_{si}}{g_{si}} - 1 \right) \frac{R_i^{\text{req}}}{g_{si}}}{M_s^{\text{upp}} - M_s^{\text{low}}} \\
\quad & \quad = R_i^{\text{req}}, \\
\quad & \quad \left( 2 \frac{r_{si}}{g_{si}} - 1 \right) \frac{R_i^{\text{req}}}{g_{si}} - \frac{M_s^{\text{upp}}}{N_s} \leq p_{si} \\
\quad & \quad \leq \left( 2 \frac{r_{si}}{g_{si}} - 1 \right) \frac{R_i^{\text{req}}}{g_{si}} - \frac{M_s^{\text{low}}}{N_s}, \\
\quad & \quad \text{and constraints (5) and (6),} \quad (8)
\end{align*}
\]

Variables: $(r_{si}, p_{si})$ and $p_{Bi(s)}$.

However, constraints (7) and (8) still yield a non-convex feasible region, leading to that Problem (OGPM) is a non-convex optimization problem. To solve Problem (OGPM) efficiently, we exploit its layered property. Specifically, we introduce an auxiliary variable $\rho_{si} \in [0, 1]$ as follows:

\[
\rho_{si} = \frac{r_{si} - M_s^{\text{upp}} + N_s p_{si} - N_s \left( 2 \frac{r_{si}}{g_{si}} - 1 \right) \frac{R_i^{\text{req}}}{g_{si}}}{M_s^{\text{upp}} - M_s^{\text{low}}} 
\]

Variable $\rho_{si}$ denotes the portion of MU $i$’s traffic requirement successfully offloaded through sAP $s$, and it is introduced to help us decompose Problem (OGPM) as shown in Figure 2. Specifically, we use $\rho_{si}$ to decompose Problem (OGPM) into a top-problem (i.e., Problem (OGPM-Top)) and two parallel subproblems (i.e., Problem (Sub-mBS) and Problem (Sub-sAP)). We next explain the details about the decomposition as follows.

Given a fixed $\rho_{si}$, we can equivalently separate Problem (OGPM) into two parallel subproblems to minimize the BS’s transmit-power and the sAP’s transmit-power, respectively.

- **Subproblem to find the BS’s minimum transmit-power as a function $\rho_{si}$**: Given $\rho_{si}$, the first subproblem aims at finding the BS’s minimum transmit-power $\hat{p}_{Bi(s)}(\rho_{si})$ as follows:

\[
\begin{align*}
\text{(Sub - mBS)} \quad & \hat{p}_{Bi(s)}(\rho_{si}) = \arg \min p_{Bi(s)} \\
\quad & \text{Subject to: } W_B \log_2 \left( 1 + \frac{p_{Bi(s)} g_{Bi}}{n_{Bi}} \right) \\
\quad & \quad = (1 - \rho_{si}) R_i^{\text{req}}, \\
\quad & \quad \text{and constraint (5),} \quad (10)
\end{align*}
\]

Variable: $p_{Bi(s)}$.

Notice that we denote the optimal solution $\hat{p}_{Bi(s)}(\rho_{si})$ (namely, the BS’s minimum transmit-power) as a function of $\rho_{si}$.

- **Subproblem to find the sAP’s minimum transmit-power as a function $\rho_{si}$**: Given $\rho_{si}$, the second subproblem aims at finding the sAP $s$’s minimum transmit-power $\hat{p}_{si}(\rho_{si})$ as follows:

\[
\begin{align*}
\text{(Sub - sAP)} \quad & \hat{p}_{si}(\rho_{si}) = \arg \min p_{si} \\
\quad & \text{Subject to: } p_{si} = \left( \frac{M_s^{\text{upp}} - M_s^{\text{low}}}{N_s} \right) \rho_{si} \frac{R_i^{\text{req}}}{g_{si}} \\
\quad & \quad + \left( 2 \frac{r_{si}}{g_{si}} - 1 \right) \frac{n_{si}}{g_{si}} - \frac{M_s^{\text{upp}}}{N_s}, \\
\quad & \quad \text{and constraints (6) and (8),} \quad (11)
\end{align*}
\]

Variables: $p_{si}$ and $r_{si}$.

Constraint (11) stems from constraint (9). We denote the optimal solution of this subproblem (i.e., the tuple of sAP $s$’s minimum transmit-power and assigned-offloading rate $(\hat{p}_{si}(\rho_{si}), \hat{r}_{si}(\rho_{si}))$) as a function of $\rho_{si}$.

By using the optimal solutions of the two subproblems at the bottom, we further optimize $\rho_{si} \in [0, 1]$ to minimize the total on-grid power consumption, which leads to Problem (OGPM-Top) as follows:

\[
\text{(OGPM - Top)} \quad \rho_{si}^* = \arg \min \hat{p}_{Bi(s)}(\rho_{si}) + \hat{p}_{si}(\rho_{si}) \\
\text{Variable: } 0 \leq \rho_{si}^* \leq 1.
\]

Notice that after we solve Problem (OGPM-Top) and find $\rho_{si}^*$, we can express the optimal solution of Problem (OGPM) by feeding $\rho_{si}^*$ into the two subproblems, i.e.,

\[
\left( \hat{p}_{Bi(s)}(\rho_{si}^*), \hat{p}_{si}(\rho_{si}^*) \right) = \left( \hat{p}_{Bi(s)}(\rho_{si}), \hat{p}_{si}(\rho_{si}), \hat{r}_{si}(\rho_{si}) \right). \quad (12)
\]

In addition, $x_{Bi(s), F}^* = R_i^{\text{req}}$, and $p_{Bi(s), F}^* = (2 \frac{r_{si}}{g_{si}} - 1) \frac{n_{Bi}}{g_{Bi}}$ (supposing that $p_{Bi(s), F}^* \leq p_{Bi(s)}^{\text{max}}$, and $p_{Bi(s), F}^* = 0$. Here, the subscript “F” denotes “Full Offloading Outage”. Due to the triviality, we assume that the full offloading outage will not happen at the optimum of Problem (OGPM).
IV. PROPOSED ALGORITHMS TO SOLVE PROBLEM (OGPM)

In this section, we propose algorithms to solve Problem (Sub-mBS), Problem (Sub-sAP), and Problem (OGPM-Top) in the above decomposition structure shown in Figure 2.

A. Analytical Solution of Problem (Sub-mBS)

We first solve Problem (Sub-mBS). By taking into account 

\[ p_{si}^{\text{max}} \] , the viable interval of \( p_{si} \) which can ensure that Problem (Sub-mBS) is feasible, is 

\[ \rho_{si} \in [\max(0, \rho_{si}^{\text{low, mBS}}), 1] \] where 

\[ \rho_{si}^{\text{low, mBS}} = 1 - \frac{W_{si}}{R_{si}} \log(1 + \frac{P_{si}^{\text{max, mBS}}}{G_{si}}) \]. 

For each \( \rho_{si} \) in this viable interval, we can derive the optimal solution of Problem (Sub-mBS) as:

\[
\hat{p}_{B_i}(s)(\rho_{si}) = \left( 2 \frac{h_{\text{req}}(1-\rho_{si})}{h_{B_i}} - 1 \right) \frac{n_{B_i}}{g_{B_i}}, \quad (13)
\]

\[
\hat{x}_{B_i}(s)(\rho_{si}) = (1 - \rho_{si})R_{i}^{\text{req}}. \quad (14)
\]

B. Proposed Algorithm to Solve Problem (Sub-sAP)

Problem (Sub-sAP) is difficult to solve due to the non-convexity of constraint (10). To overcome this difficulty, we transform Problem (Sub-sAP) into the following form with a single decision-variable \( r_{si} \):

\[
\text{(Sub-sAP-E)} \quad \hat{p}_{si}(\rho_{si}) = \min \left( M_{s}^{\text{upp}} - M_{s}^{\text{low}} \right) \frac{\rho_{si} R_{i}^{\text{req}}}{N_{s} \rho_{si}} + (2 - \frac{h_{si}}{W_{si}}) \frac{n_{si}}{g_{si}} - \frac{M_{s}^{\text{upp}} - M_{s}^{\text{low}}}{N_{s} \rho_{si}} \right), \quad (15)
\]

Variable: \( r_{si} \geq \rho_{si} R_{i}^{\text{req}} \).

Notice that the first “\( \leq \)” in constraint (8) can be directly satisfied by using (11) to replace \( p_{si} \), and the second “\( \leq \)” in (8) translates to (15). Compared with Problem (Sub-sAP), we temporarily do not consider constraint (6) in Problem (Sub-sAP-E). Thanks to this temporal relaxation, Problem (Sub-sAP-E) becomes a convex optimization problem (which will be explained in Proposition 1 below). Before that, we discuss the connections between Problems (Sub-mBS) and (Sub-sAP-E).

Remark 1 [Connections Between Problem (Sub-sAP) and Problem (Sub-sAP-E)]: Problem (Sub-sAP-E) is equivalent to Problem (Sub-sAP), except that we do not include constraint (6). As a result, there will be three possible outcomes after we solve Problem (Sub-sAP-E):

- First, if the optimal solution of Problem (Sub-sAP-E) (i.e., \( \hat{p}_{si}(\rho_{si}) \)) satisfies \( 0 \leq \hat{p}_{si}(\rho_{si}) \leq p_{si}^{\text{max}} \), then \( \hat{p}_{si}(\rho_{si}) \) suffices to be the optimal solution of Problem (Sub-sAP).

- Second, if the optimal solution of Problem (Sub-sAP-E) (i.e., \( \hat{p}_{si}(\rho_{si}) \)) satisfies \( \hat{p}_{si}(\rho_{si}) > p_{si}^{\text{max}} \) then Problem (Sub-sAP) is infeasible under the currently given \( \rho_{si} \).

- Third, if \( \hat{p}_{si}(\rho_{si}) < 0 \), then it means that sAP’s \( r_{si} \) can be completely supported by its harvested energy, and there is no need for sAP to spend any positive on-grid power.

In this case, additional operations are required such that we can find \( \hat{p}_{si}(\rho_{si}) = 0 \) (we will specify the details later on).

To solve Problem (Sub-sAP-E), we identify the following important property.

**Proposition 1**: Problem (Sub-sAP-E) is a convex optimization problem.

Proof: Let \( F(r_{si}) \) denote the first-order derivative of the objective function of Problem (Sub-sAP-E). We then can derive:

\[
F(r_{si}) = \ln 2n_{si} 2 \frac{\rho_{si} R_{i}^{\text{req}}}{N_{s} \rho_{si}} - \frac{M_{s}^{\text{upp}} - M_{s}^{\text{low}}}{N_{s} \rho_{si}} r_{si}^{2} - \frac{2n_{si}}{N_{s} \rho_{si}}, \quad (16)
\]

which is monotonically increasing in \( r_{si} \). Moreover, the feasible interval of Problem (Sub-sAP-E) is affine. Thus, Problem (Sub-sAP-E) is a convex optimization problem [35].

Proposition 1 enables us to use the Karush-Kuhn-Tucker (KKT) conditions [35] to compute the optimal solution of Problem (Sub-sAP-E). Specifically, we use \( r_{si}(\rho_{si}) \) to denote the optimal solution of Problem (Sub-sAP-E), which depends on the given \( \rho_{si} \). To find \( r_{si}(\rho_{si}) \), we propose SubSol-Algorithm (the details are shown in the next page). The key of SubSol-Algorithm is to exploit the increasing property of \( F(r_{si}) \) (according to the proof of Proposition 1) and use the bisection-search to find the critical value (denoted by \( r_{si}^{\text{opt, temp}} \)) such that \( F(r_{si}^{\text{opt, temp}}) = 0 \). The WHILE-Loop (from Step 7 to Step 17) shows the bisection-search method. Since \( r_{si} \) is lower bounded by \( \rho_{si} R_{i} \) according to (15), we directly set \( r_{si}^{\text{opt, temp}} = \rho_{si} R_{i} \) if \( F_{\text{Case1}}(\rho_{si} R_{i}) > 0 \), i.e., Steps 4-5 in SubSol-Algorithm. Finally, SubSol-Algorithm outputs \( r_{si}(\rho_{si}) = r_{si}^{\text{opt, temp}} \). Notice that based on \( r_{si}(\rho_{si}) \), SubSol-Algorithm also outputs the smallest transmit-power required by sAP in Step 19 (i.e., the optimal objective function value of Problem (Sub-sAP-E)) as follows:

\[
\hat{p}_{si}(\rho_{si}) = \left( M_{s}^{\text{upp}} - M_{s}^{\text{low}} \right) \frac{\rho_{si} R_{i}^{\text{req}}}{N_{s} \hat{r}_{si}(\rho_{si})} + (2 - \frac{h_{si}}{W_{si}}) \frac{n_{si}}{g_{si}} - \frac{M_{s}^{\text{upp}} - M_{s}^{\text{low}}}{N_{s} \hat{r}_{si}(\rho_{si})} \right), \quad (17)
\]

**Viability of SubSol-Algorithm to Solve Problem (Sub-sAP)**: We illustrate the viability of SubSol-Algorithm to solve Problem (Sub-sAP) by addressing the three cases in Remark 1.

- First, \( \hat{p}_{si}(\rho_{si}), \hat{r}_{si}(\rho_{si}) \) (i.e., the output of SubSol-Algorithm) suffices to be the optimal solution of Problem (Sub-sAP), if \( \hat{p}_{si}(\rho_{si}) \) satisfies \( 0 \leq \hat{p}_{si}(\rho_{si}) \leq p_{si}^{\text{max}} \).

- Second, Problem (Sub-SAP) is infeasible (under the given \( \rho_{si} \)), if \( \hat{p}_{si}(\rho_{si}) > p_{si}^{\text{max}} \).

- Third, if \( \hat{p}_{si}(\rho_{si}) < 0 \), it means that there is no need for sAP to spend any positive on-grid power. In this case, we need additional operations to find the proper value of \( r_{si}^{\text{opt, temp}} \) that yields \( p_{si}^{\text{opt, temp}} = 0 \). To this end, we design the additional Steps 20-31 in SubSol-Algorithm.

We exploit the property that \( \frac{(M_{s}^{\text{upp}} - M_{s}^{\text{low}}) p_{si}^{\text{req}}}{N_{s} \hat{r}_{si}(\rho_{si})} + (2 - \frac{h_{si}}{W_{si}}) \frac{n_{si}}{g_{si}} \) is increasing for \( \hat{r}_{si} \in [\hat{r}_{si}^{\text{thr}}, \infty] \) (here, \( \hat{r}_{si}^{\text{thr}} \) is equal to \( r_{si}^{\text{opt, temp}} \) obtained in Step 9 of SubSol-Algorithm). Hence, we use the bisection-search to find the new \( r_{si}^{\text{opt, temp}} \) that yields \( p_{si}^{\text{opt, temp}} = 0 \).
SubSol-Algorithm: To Compute $\tilde{r}_{si}(\rho_{si})$ and $\tilde{p}_{si}(\rho_{si})$

1: Input: $\rho_{si}$.
2: MU i sets $\gamma$ (i.e. the tolerable computation-error used in the bisection-search) as a very small number and sets flag = 1.
3: MU i sets $r_{si}^{\text{lower}} = \rho_{si} R_{si}^{\text{req}}$ and sets $r_{si}^{\text{upper}} = r_{si}^{\text{upper}}$ (where $r_{si}^{\text{upper}}$ is a very large number).
4: if $F(r_{si}^{\text{lower}}) > 0$ then
5: MU i sets $r_{si}^{\text{opt, temp}} = r_{si}^{\text{lower}}$.
6: else
7: while flag = 1 do
8: if $(r_{si}^{\text{upper}} - r_{si}^{\text{lower}}) \leq \gamma$ then
9: MU i sets $r_{si}^{\text{opt, temp}} = \frac{1}{2}(r_{si}^{\text{lower}} + r_{si}^{\text{upper}})$ and flag = 0.
10: else
11: if $F\left(\frac{1}{2}(r_{si}^{\text{lower}} + r_{si}^{\text{upper}})\right) > 0$ then
12: MU i sets $r_{si}^{\text{upper}} = \frac{1}{2}(r_{si}^{\text{lower}} + r_{si}^{\text{upper}})$.
13: else
14: MU i sets $r_{si}^{\text{lower}} = \frac{1}{2}(r_{si}^{\text{lower}} + r_{si}^{\text{upper}})$.
15: end if
16: end if
17: end while
18: end if
19: MU i computes $p_{si}^{\text{opt, temp}} = \frac{(M_{si}^{\text{upper}} - M_{si}^{\text{lower}}) p_{si} R_{si}^{\text{req}}}{N_{si}^{\text{upper}} r_{si}^{\text{opt, temp}}} + (2 \frac{r_{si}^{\text{opt, temp}}}{W_{si}} - 1)\frac{\Delta_{si}}{N_{si}}$.
20: if $p_{si}^{\text{opt, temp}} \leq \rho_{si}$ then
21: MU i sets $\tau = r_{si}^{\text{opt, temp}}$ and $\tau = r_{si}^{\text{upper}}$.
22: while $(\tau - \frac{\rho_{si}}{2}) > \gamma$ do
23: MU i sets $v = \frac{2(M_{si}^{\text{upper}} - M_{si}^{\text{lower}}) p_{si} R_{si}^{\text{req}}}{N_{si}^{\text{upper}}(\tau + \frac{\rho_{si}}{2})} + (2 \frac{\rho_{si}}{W_{si}} - 1)\frac{\Delta_{si}}{N_{si}}$.
24: if $v > 0$ then
25: MU i sets $\tau = \frac{1}{2}(\tau + \frac{\rho_{si}}{2})$.
26: else
27: MU i sets $\tau = \frac{1}{2}(\tau + \frac{\rho_{si}}{2})$.
28: end if
29: end while
30: MU i sets $r_{si}^{\text{opt, temp}} = \frac{1}{2}(\tau + \frac{\rho_{si}}{2})$, and $p_{si}^{\text{opt, temp}} = \frac{(M_{si}^{\text{upper}} - M_{si}^{\text{lower}}) p_{si} R_{si}^{\text{req}}}{N_{si}^{\text{upper}} r_{si}^{\text{opt, temp}}} + (2 \frac{r_{si}^{\text{opt, temp}}}{W_{si}} - 1)\frac{\Delta_{si}}{N_{si}}$.
31: end if
32: Output: $\tilde{r}_{si}(\rho_{si}) = r_{si}^{\text{opt, temp}}$ and $\tilde{p}_{si}(\rho_{si}) = p_{si}^{\text{opt, temp}}$.

C. Proposed Algorithm to Solve Problem (OGPM-Top)

After solving Problem (Sub-mBS) and Problem (Sub-sAP) and obtaining $\hat{p}_{B_{i}(\rho_{si})}$ and $\hat{p}_{si}(\rho_{si})$, respectively, we continue to solve Problem (OGPM-Top). In spite of its simple form, it is difficult to solve Problem (OGPM-Top), since we still cannot analytically derive $\hat{p}_{B_{i}(\rho_{si})}$ and $\hat{p}_{si}(\rho_{si})$.

Fortunately, Problem (OGPM-Top) only involves a single-variable $\rho_{si}$ within a fixed interval, i.e., $\rho_{si} \in [0, 1]$. Based on this property, we propose LS-Algorithm that performs a linear-search of $\rho_{si}$ in [0, 1] (with a very small step-size) to solve Problem (OGPM-Top) and find the optimal solution $(\tilde{r}_{si}^{*}, p_{si}^{*}, x_{B_{i}(\rho_{si})}^{*})$. The details of LS-Algorithm are as follows.

D. Advanced Algorithm to Solve Problem (OGPM-Top) Based on the Case of Zero-Outage

The linear-search in LS-Algorithm requires a very small step-size $\Delta$ (e.g., $\Delta = 10^{-5}$), which consequently requires at most $\frac{1}{\Delta}$ iterations. To reduce the number of iterations, we further propose an advanced LS-Algorithm (i.e., ADLS-Algorithm) in this subsection. The key idea is to identify a range of $\rho_{si}$ over which we can analytically characterize the optimal solution of Problem (OGPM-Top). As a result, we do not need to use the above-linear-search within this range.

1) Zero-Outage Case and Its Sufficient Condition to Occur: To find such an interval of $\rho_{si}$ over which we do not need to execute the linear-search, we identify a special case of zero-outage, namely, $P_{out}(\tilde{r}_{si}(\rho_{si}), r_{si}) = 0$. As an important property, we provide the following proposition.

Proposition 2: Given $\rho_{si}$, if $F(\rho_{si} R_{si}^{\text{req}}) \geq 0$, then the optimal solution of Problem (Sub-sAP-E) yields the zero-outage, i.e., $P_{out}(\tilde{p}_{si}(\rho_{si}), r_{si}(\rho_{si})) = 0$.

Proof: Based on the convexity of Problem (Sub-sAP-E), if $F(\rho_{si} R_{si}^{\text{req}}) \geq 0$, then the optimal solution can be directly expressed as $\tilde{r}_{si}(\rho_{si}) = \rho_{si} R_{si}^{\text{req}}$, which consequently leads to $\tilde{p}_{si}(\rho_{si}) = \frac{2 \rho_{si} R_{si}^{\text{req}}}{W_{si}} - 1)\frac{\Delta_{si}}{N_{si}} - M_{si}^{\text{low}}$. By substituting $(\tilde{r}_{si}(\rho_{si}), \tilde{p}_{si}(\rho_{si}))$ into (3), we can obtain $P_{out}(\tilde{r}_{si}(\rho_{si}), \tilde{p}_{si}(\rho_{si})) = 0$.

Furthermore, we identify the following important property.

Proposition 3: There exists a critical threshold $\rho_{si}^{\text{cri}}$, which is given by

$$\rho_{si}^{\text{cri}} = \frac{W_{si}}{R_{si}^{\text{req}}} \ln 2 \sqrt{\frac{M_{si}^{\text{upper}} - M_{si}^{\text{low}}}{N_{si}}} $$

Here, function $\mathcal{W}(.)$ is the Lambert W-function [36], i.e., the inverse function of $f(x) = x \exp(x)$. Specifically, if $\rho_{si}^{\text{cri}} < 1$, then for each $\rho_{si} \in [0, 1]$, the corresponding optimal solution $(\tilde{p}_{si}(\rho_{si}), \tilde{r}_{si}(\rho_{si}))$ of Problem (Sub-sAP-E) leads to the zero-outage.

Proof: Based on (16), we can derive $F(\rho_{si} R_{si}^{\text{req}}) = \ln 2 \frac{\Delta_{si}}{N_{si}} - \frac{M_{si}^{\text{upper}} - M_{si}^{\text{low}}}{N_{si}} \rho_{si} R_{si}^{\text{req}}$, which is increasing in $\rho_{si}$. Thus, there exists a unique $\rho_{si}^{\text{cri}}$ such that $F(\rho_{si}^{\text{cri}} R_{si}^{\text{req}}) = 0$. By solving $F(\rho_{si}^{\text{cri}} R_{si}^{\text{req}}) = 0$, we can obtain $\rho_{si}^{\text{cri}}$ in (18). 2

2) Analytical Solution in Zero-Outage Case: The purpose of analyzing the zero-outage case is that we can analytically
derive the optimal solution of Problem (OGPM). The details are as follows. With $P_{out}(p_{si}, r_{si}) = 0$, Problem (OGPM) can be equivalently re-written into the following form (where, the letter “Z” denotes “Zero”):

\[
\begin{align*}
\text{(OGPM – Z)} & \min \ p_{Bi(s)} + p_{si} \\
\text{Subject to:} & \ W_B \log_2 \left( 1 + \frac{p_{Bi(s)} g_{Bi}}{n_{Bi}} \right) + r_{si} = R_{i}^{req} \\
& p_{si} \geq \left( \frac{2}{w_{si}} - 1 \right) \frac{n_{si}}{N_{s}} \frac{M_{s}^{low}}{N_{s}} \\
& \text{and constraints (5) and (6)} \\
\text{Variable:} & \ \{ r_{si}, p_{si} \} \text{ and } p_{Bi} 
\end{align*}
\]

(19)

We next analytically derive the optimal solution of Problem (OGPM-Z). To this end, we firstly identify the following two subcases regarding the right hand side of (19):

- **Subcase-I** which is based on the pre-assumption that $r_{si} \leq W_B \log_2(1 + \frac{M_{s}^{low}}{N_{s} n_{si}})$. Subcase-I means that the assigned offloading rate $r_{si}$ is no larger than the rate that can be solely supported by sAP s’s minimum EH power-supply $M_{s}^{low}$, which thus ensures the zero-outage to occur. Correspondingly, $p_{si}$ should be zero.

- **Subcase-II** which is based on the pre-assumption that $r_{si} \geq W_B \log_2(1 + \frac{M_{s}^{low}}{N_{s} n_{si}})$. Subcase-II means that the assigned offloading rate $r_{si}$ is larger than the rate that can be solely supported by sAP s’s minimum EH power-supply $M_{s}^{low}$. As a result, a positive $p_{si}$ is required to ensure the zero-outage to occur.

Based on the above Subcase-I and Subcase-II, we derive the optimal solution of Problem (OGPM-Z) under the two subcases as follows.

**Solution under Subcase-I:** Based on the rationale of Subcase-I, the optimal solution of Problem (OGPM-Z) can be written as:

\[
\begin{align*}
\hat{r}_{si,Z}^{\text{SubI}} &= \min \left\{ W_B \log_2 \left( 1 + \frac{M_{s}^{low}}{N_{s} n_{si}} \right), R_{i}^{req} \right\} \\
p_{si,Z}^{\text{SubI}} &= 0, \\
\hat{x}_{B_i(s),Z}^{\text{SubI}} &= R_{i}^{req} - \hat{r}_{si,Z}^{\text{SubI}} \\
p_{Bi}^{\text{SubI}} &= \frac{n_{Bi}}{g_{Bi}} 
\end{align*}
\]

Notice that Subcase-I is valid, only if $p_{Bi(s),Z}^{\text{SubI}} \leq p_{Bi}^{max}$.

**Solution under Subcase-II:** Based on the rationale of Subcase-II, we can derive the optimal solution of Problem (OGPM-Z) as follows. Since constraint (19) is strictly binding at the optimum in this case (i.e., no additional on-grid power is required), we can equivalently transform Problem (OGPM-Z-SubII) into a single-variable optimization problem as follows:

\[
\begin{align*}
\text{(OGPM – Z – SubII)} & \min \left\{ \frac{2}{w_{si}} - 1 \right\} \frac{n_{si}}{g_{si}} \frac{M_{s}^{low}}{N_{s}} \\
& + \left( \frac{2}{w_{Bi}} - 1 \right) \frac{n_{Bi}}{g_{Bi}} \\
\text{Variable:} & \ \hat{r}_{si,Z}^{\text{SubII}} \leq r_{si} \leq \hat{r}_{si,Z}^{\text{SubII}} 
\end{align*}
\]

In the above problem, the lower-bound $r_{si,Z}^{low} \leq \hat{r}_{si,Z}^{\text{SubII}}$ is given by:

\[
\begin{align*}
r_{si,Z}^{low} &= \max \left\{ R_{i}^{req} - W_B \log_2 \left( 1 + \frac{M_{s}^{low}}{W_{s} g_{si}} \right), W_{s} \log_2 \left( 1 + \frac{M_{s}^{low}}{N_{s} n_{si}} \right), R_{i}^{req} \right\},
\end{align*}
\]

which stems from (5) and $p_{si} = (2 \frac{r_{si}}{w_{si}} - 1) \frac{n_{si}}{N_{s}} - \frac{M_{s}^{low}}{N_{s}} \geq 0$. The upper-bound $r_{si,Z}^{upp} \geq \hat{r}_{si,Z}^{\text{SubII}}$ is given by:

\[
\begin{align*}
r_{si,Z}^{upp} &= \min \left\{ W_{s} \log_2 \left( 1 + \frac{p_{max}}{n_{si}} \frac{M_{s}^{low}}{N_{s}} \right), R_{i}^{req} \right\},
\end{align*}
\]

which stems from $p_{si} = (2 \frac{r_{si}}{w_{si}} - 1) \frac{n_{si}}{N_{s}} - \frac{M_{s}^{low}}{N_{s}} \leq p_{max}$.

Notice that Subcase-II is valid, only if $r_{si,Z}^{low} \geq r_{si,Z}^{upp}$. Otherwise, Subcase-II fails to hold.

In particular, we express the optimal solution of Problem (OGPM-Z-SubII) in the following proposition.

**Proposition 4:** For $r_{si,Z}^{low} \leq r_{si,Z}^{upp}$, the optimal solution of Problem (OGPM-Z-SubII) can be analytically written as:

\[
\begin{align*}
r_{si,Z}^{\text{SubII}} &= \begin{cases} 
\hat{r}_{si,Z}^{\text{SubII}} & \text{if } F_{Z} \left( r_{si,Z}^{\text{SubII}} \right) > 0 \\
\hat{r}_{si,Z}^{\text{SubII}} & \text{if } F_{Z} \left( r_{si,Z}^{\text{SubII}} \right) < 0 \\
\hat{r}_{si,Z}^{\text{SubII}} & \text{otherwise}
\end{cases}
\end{align*}
\]

Here, $F_{Z}(r_{si}) = \ln \left( \frac{2 \ln N_{s} + 2 \frac{r_{si}}{w_{si}} \frac{M_{s}^{low}}{W_{s} g_{si}}}{2 \ln N_{s} + 2 \frac{r_{si}}{w_{si}} \frac{M_{s}^{low}}{W_{s} g_{si}} + 2 \frac{r_{si}}{w_{si}} - 1} \right)$ is the first-order derivative of the objective function of Problem (OGPM-Z-SubII).

**Proof:** It can be verified that function $F_{Z}(r_{si})$ is increasing in $r_{si}$. Thus, considering the affine feasible interval, Problem (OGPM-Z-SubII) is a strictly convex optimization problem. The convexity enables us to use the KKT conditions to derive the optimal solution. Specifically, by solving $F_{Z}(r_{si}) = 0$, we obtain the last case of (20). On the other hand, if $F_{Z} \left( r_{si,Z}^{\text{SubII}} \right) > 0$ (which means that the objective function is increasing for $r_{si} \in \left[ r_{si,Z}^{low} \right]$), we set $r_{si,Z}^{\text{SubII}} = r_{si,Z}^{low}$, i.e., the first case of (20). Finally, if $F_{Z} \left( r_{si,Z}^{\text{SubII}} \right) < 0$ (which means that the objective function is decreasing for $r_{si} \in \left[ r_{si,Z}^{upp} \right]$), we set $r_{si,Z}^{\text{SubII}} = r_{si,Z}^{upp}$, i.e., the second case of (20).

By using $\hat{r}_{si,Z}^{\text{SubII}}$ in (20), we derive the optimal solution of Problem (OGPM-Z-SubII) as follows:

\[
\begin{align*}
p_{si,Z}^{\text{SubII}} &= \frac{2}{w_{si}} \frac{r_{si,Z}^{\text{SubII}} - 1}{w_{si}} \frac{n_{si}}{g_{si}} - \frac{M_{s}^{low}}{N_{s}} \\
x_{B_i(s),Z}^{\text{SubII}} &= R_{i}^{req} - \hat{r}_{si,Z}^{\text{SubII}} \\
p_{Bi}^{\text{SubII}} &= \frac{2}{w_{Bi}} \frac{r_{si,Z}^{\text{SubII}} - 1}{w_{Bi}} \frac{n_{Bi}}{g_{Bi}}.
\end{align*}
\]
In summary, by comparing the optimal solutions under Subcase-I and Subcase-II (if they are feasible), we can derive the optimal solution of Problem (OGPM-Z) as follows:

\[
(r_{s1}^*, P_{s1}^*, Z_{s1}^*, x_{s1}^*, z_{s1}^*, p_{B_i(s)}^*) = (r_{s1}, Z - \hat{\theta} P_{s1}, Z - \hat{\theta} x_{s1}, Z - \hat{\theta} z_{s1}, Z - \hat{\theta} p_{B_i(s)}, Z - \hat{\theta} x_{s1})
\]

(21)

where \(\hat{\theta} = \arg \min_{\theta \in \{1,2,3,4\}} P_{s1}^*, Z - \hat{\theta} p_{B_i(s)}^*\) (recall that \(\gamma\) denotes the tolerable computation-error used by our SubSol-Algorithm before).

Proposed Advanced LS-Algorithm: Based on Propositions 2 and 3, for the interval of \(x_{s1} \in [\rho_{s1}^{\text{cri}}, 1]\) (within which the optimal solution of Problem (OGPM) always leads to the zero-outage), we can directly use (21) to compute the optimal solution of Problem (OGPM), instead of executing a linear-search \(\rho_{s1} \in [\rho_{s1}^{\text{cri}}, 1]\). Exploiting this important property, we further propose the following ADLS-Algorithm ("AD" means "Advanced") to solve Problem (OGPM). The details of ADLS-Algorithm are shown on the next page.

Compared with LS-Algorithm, ADLS-Algorithm uses (21) to compute the optimal solution for the interval \(x_{s1} \in [\rho_{s1}^{\text{cri}}, 1]\) (i.e., Steps 3-9), and thus avoids the linear-search of \(x_{s1} \in [\rho_{s1}^{\text{cri}}, 1]\). In particular, let \(N\) denote the step-size (which is a very small number, e.g., \(10^{-5}\)) used by the linear-search in ADLS-Algorithm. Our proposed ADLS-Algorithm requires no more than \(2\log_2(\frac{\text{upper}}{\text{lower}})\) (recall that \(\gamma\) denotes the tolerable computation-error used by our SubSol-Algorithm before). In Section VI, Figure 5(b) shows the advantage of ADLS-Algorithm in reducing the number of iterations.

Until now, we have completed solving Problem (OGPM) and obtained the optimal offloading solution for the targeted pair of sAP \(s\) and MU \(i\), when sAP \(s\) is serving the total number of \(N_s\) MUs. Notice that by using our ADLS-Algorithm, we can find the optimal offloading solution for an arbitrary sAP-MU pair, which facilitates our extended study of the multi-sAP case in the next section.

V. EXTENSION TO THE SCENARIO OF MULTIPLE SMALL CELLS

A. System Model and Problem Formulation

In this section, based on the optimal offloading solution for the single sAP case in Section IV, we further extend to investigate the scenario of multiple sAPs. As shown in the system model in Figure 1, we consider a scenario of a group of sAPs \(S = \{1, 2, \ldots, S\}\) providing the DC-enabled offloading to a group of MUs \(I = \{1, 2, \ldots, I\}\). Our objective is to investigate how the sAPs properly select different MUs to provide the DC-enabled offloading, with the objective of maximizing the total network-reward. To model this problem, we introduce the binary variable \(z_{si} \in \{0, 1\}\) for every \(s \in S, i \in I\). We denote whether sAP \(s\) selects MU \(i\) or not. Specifically, \(z_{si} = 1\) means that sAP \(s\) selects MU \(i\) to execute the DC-enabled traffic offloading, while \(z_{si} = 0\) means the opposite.

Recall that in Sections III and IV, by assuming that sAP \(s\) selects exactly \(N_s = \sum_{i \in I} z_{si}\) MUs to serve, we have proposed ADLS-Algorithm (and LS-Algorithm) to compute the optimal traffic scheduling and power allocation for the pair of sAP \(s\) and MU \(i\), which is denoted by \((r_{s1}^*, P_{s1}^*, z_{s1}^*, x_{s1}^*, p_{B_i(s)}^*)\).

Adls-Algorithm: The Optimal Solution \((r_{s1}^*, P_{s1}^*, z_{s1}^*, x_{s1}^*, p_{B_i(s)}^*)\) of Problem (OGPM)

1: Initialization: Set \(\rho_{s1} = 0\) and \(\Delta = \text{a sufficiently small number (} \Delta = 10^{-5}\))
2: while \(\rho_{s1} < 1\) do
3: if \(\rho_{s1} \geq \rho_{s1}^{\text{cri}}\) then
4: \(\text{compute } (r_{s1}^*, P_{s1}^*, z_{s1}^*, x_{s1}^*, p_{B_i(s)}^*) \text{ according to (21)} \)
5: end if
6: MU \(i\) updates CBV \(= p_{s1}^* z_{s1}^* + p_{B_i(s)}^* z_{s1}^*\)
7: end while
8: MU \(i\) sets CBS = \((r_{s1}^*, P_{s1}^*, z_{s1}^*, x_{s1}^*, p_{B_i(s)}^*)\)
9: output \((r_{s1}^*, P_{s1}^*, z_{s1}^*, x_{s1}^*, p_{B_i(s)}^*)\) = CBS.

Based on (22), we formulate the following optimal MU-selection problem to investigate how different sAPs optimally select different MUs to provide the DC-enabled offloading:

(MultiMUSel):

\[
\max \sum_{s \in S, i \in I} \left(\mu R_{i}^{\text{req}} - \pi(p_{s1}, (\sum_{i \in I} z_{si})) + p_{B_i(s)}^*(\sum_{i \in I} z_{si})\right)
\]

subject to:\n
\[
\sum_{s \in S} z_{si} \leq 1, \forall i \in I
\]

\[
\sum_{i \in I} z_{si} \leq H_{s}^{\text{max}}, \forall s \in S
\]

\[
z_{si} = 0, \text{ if } i \in \Omega^{\text{inf}}_{s}(\sum_{i \in I} z_{si}), \forall s \in S
\]

Variables: \((z_{si})_{s \in S, i \in I}\)

In Problem (MultiMUSel), we aim at maximizing the total network-reward that takes into account the marginal reward \(\lambda\) for successfully serving a MU’s traffic requirement, and the cost due to the mBS’s and sAP’s total on-grid power.
consumption \( (p^s_{si} \sum_{i \in I} z_{si} + p_{Bi}(s) \sum_{i \in I} z_{si}) \) when sAP \( s \) selects MU \( i \) to provide the traffic offloading. Here, parameter \( \pi \) denotes the marginal cost for the on-grid power consumption. Constraint (23) means that MU \( i \) can only be served by at most one sAP. Constraint (24) means that sAP \( s \) can select no more than \( H_s^{\max} \) MUs to serve. Here, we consider that the small cells use the frequency division multiple access (FDMA) to accommodate different MUs, and each sAP has \( H_s^{\max} \) available sub-channels to serve the MUs. In constraint (25), set \( f_{s,s}^{\inf}(\sum_{i \in I} z_{si}) \) denotes the subset of the MUs who cannot be served by sAP \( s \) when sAP \( s \) selects total \( \sum_{i \in I} z_{si} \) MUs to serve.5

Problem (MultiMUSel) is very challenging to solve, since it is a nonlinear binary programming problem due to the following two reasons. First, in the objective function, for each pair of sAP \( s \) and MU \( i \), the minimum on-grid power \( \min_{s} (p^s_{si} \sum_{i \in I} z_{si} + p_{Bi}(s) \sum_{i \in I} z_{si}) \) depends on the value of \( \sum_{i \in I} z_{si} \). Second, constraints (23) and (24) together lead to a resource-constrained generalized assignment problem [38]. Specifically, each sAP \( s \) (i.e., an agent) can accept no more than \( H_s^{\max} \) MUs (i.e., the jobs), and each MU \( i \) can only be assigned to at most one sAP. To tackle this difficulty, we propose an efficient algorithm to solve Problem (MultiMUSel) in the next subsection.

B. Layered Algorithm to Solve Problem (MultiMUSel)

To solve Problem (MultiMUSel), we first identify the following property. In Problem (MultiMUSel), the objective function and constraints are separable with respect to individual sAP, except that constraint (23) couples all sAPs.

To decouple (23), for each sAP \( s \), we first introduce set \( \Lambda_s \subseteq I \) to denote the subset of the MUs who are assigned to sAP \( s \) as the candidate-users to be served. Please notice that the MUs in \( \Lambda_s \) are the candidate-users to be selected by sAP \( s \) (in other words, it might be optimal for sAP \( s \) to only select some MUs in \( \Lambda_s \), instead of all of them). In addition, we introduce \( A_0 \) to denote the subset of MUs who are not assigned to any sAP (i.e., the MUs \( A_0 \) will be not served by any sAP). We impose the following two constraints regarding \( \{A_s\}_{s \in S} \), i.e., (i) \( \bigcup_{s \in S} \Lambda_s = I \), and (ii) \( \Lambda_s \cap \Lambda_{s'} = \emptyset \) for any two different \( s \) and \( s' \).

Based on \( \{A_s\}_{s \in S} \), our key idea to solve Problem (MultiMUSel) is to vertically decompose it into the following two problems as shown in Figure 3. We explain the details about the decomposition as follows.

1) Subproblem to Optimize the MU-Selection for Each Individual sAP Under Given \( \Lambda_s \): Suppose that \( \{A_s\}_{s \in S} \) is given. We solve the following subproblem for each sAP \( s \):

\[(\text{MultiMUSel-sAPs}): \text{RW}_s(\Lambda_s) = \max_{\{A_s\}_{s \in S}} \left( \sum_{i \in A_s} \left( \mu R_i^\text{req} - \pi p^s_{si} \sum_{i \in I} z_{si} + \left( p_{Bi}(s) \sum_{i \in I} z_{si} \right) \right) z_{si} \right) \]

3Notice that we can determine set \( \Omega_{s,s}^{\inf}(\sum_{i \in I} z_{si}) \) as follows. Given the value of \( \sum_{i \in I} z_{si} \), MU \( i \) belongs to set \( \Omega_{s,s}^{\inf}(\sum_{i \in I} z_{si}) \) if we find that Problem (OGPM) is infeasible for the pair of sAP \( s \) and MU \( i \).
subproblem under the given \( n \) (as well as the given \( \Lambda_s \)):

\[
RW^\text{sub}_{s}(\Lambda_s, n) = \max_{i \in \Lambda_s} \left( \mu H^\text{req}_i - \pi \left( p^*_s, \{ |H^\text{max}_s, n| \} \right) + p^*_B,(s), \{ |H^\text{max}_s, n| \} \right) z_{s_i}
\]

Subject to:

\[
\sum_{i \in \Lambda_s} z_{s_i} = \min \{ H^\text{max}_s, n \},
\]

\[
z_{s_i} = 0, \quad \text{if } i \notin \Omega^\text{inf}_s, \{ |H^\text{max}_s, n| \},
\]

Variables: \( z_{s_i} = \{ 0, 1 \}, \quad i \in \Lambda_s. \)

Since the value of \( \min \{ H^\text{max}_s, n \} \) is known, Problem (sAPS-Sub) is a linear binary programming problem, which differs from Problem (MultiMUSel-sAPs). We will show that we can analytically derive \( RW^\text{sub}_{s}(\Lambda_s, n) \) and thus solve Problem (sAPS-Sub).

1) **Top-Problem (sAPS-Top)** to Optimize \( n \): After obtaining \( RW^\text{sub}_{s}(\Lambda, n) \) for the given \( n \), we then solve the following problem to find the optimal \( n^* \) that can maximize sAP’s reward under the given set \( \Lambda_s \):

\[
RW_s(\Lambda_s) = \max_{n=\{0,1,2,\ldots,\min\{|\Lambda_s|, H^\text{max}_s\}\}} RW^\text{sub}_{s}(\Lambda_s, n).
\]

(28)

Notice that after solving Problem (sAPS-Top), we complete solving the original Problem (MultiMUSel-sAPs).

**D. Proposed Algorithm to Problem (MultiMUSel-sAPs) for Each sAP s**

Based on the decomposition of Problem (MultiMUSel-sAPs) explained in the previous subsection, we next solve Problem (MultiMUSel-sAPs). Specifically, we first analytically solve Problem (sAPS-Sub), and then propose an algorithm to solve Problem (sAPS-Top) by using the analytical solution of Problem (sAPS-Sub).

1) **Analytical Solution of Problem (sAPS-Sub)**: We first focus on solving Problem (sAPS-Sub) and deriving \( RW^\text{sub}_{s}(\Lambda_s, n) \). Thanks to the simple structure of Problem (sAPS-Sub), we can derive the optimal solution as follows. Specifically, suppose that the MUs in \( \Lambda_s \) are ordered in the descending order based on the value of \( V_m = \mu H^\text{req}_m - \pi(p^*_s, \{ |H^\text{max}_s, n| \} + p^*_B,(s), \{ |H^\text{max}_s, n| \}) \), i.e.,

\[
V_1 > V_2 > V_3 > \cdots > V_{|\Lambda_s|}.
\]

(29)

In the reminder of this section, we assume that MU \( m \) in \( \Lambda_s \) has been ordered according to (29) when we use subscript \( m \) to denote the MU. We provide the following result regarding the optimal solution of Problem (sAPS-Sub).

**Proposition 5**: Based on the ordering in (29), the optimal solution of Problem (sAPS-Sub) (with the given \( n \leq \min\{|\Lambda_s|, H^\text{max}_s\}\)) can be given by

\[
z^*_s,(m, n) = \begin{cases} 1, & \text{if } m \notin \Omega^\text{inf}_s, \{ |H^\text{max}_s, n| \} \text{ and } \sum_{j \in \Lambda_s, j \neq m} z^*_j < \min \{ H^\text{max}_s, n \} \vspace{0.5cm} \\
0, & \text{otherwise} \end{cases}
\]

Please notice that the subscript \( (n) \) in \( z^*_s,(m, n) \) indicates that the optimal solution depends on the given value of \( n \). On the other hand, Problem (sAPS-Sub) is infeasible, if the following condition holds:

\[
|\Lambda_s| - |\Omega^\text{inf}_s, \{ |H^\text{max}_s, n| \} | < \min \{ H^\text{max}_s, n \}.
\]

(30)

**Proof**: Due to the structure of Problem (sAPS-Sub), we can prove (30) by showing the contradiction. Let \( \{ z^*_m \} m \in \Lambda_s \) denote the optimal solution of Problem (sAPS-Sub) but being inconsistent with (30). In other words, there exists two different \( m \) and \( m' \) (with \( m < m' \) and \( m, m' \in \Lambda_s \), and \( m' > m \)) in \( \Lambda_s \), \( \Omega^\text{inf}_s, \{ |H^\text{max}_s, n| \} \) and \( \Omega^\text{inf}_s, \{ |H^\text{max}_s, n| \} \), and we have \( z^*_m = 0 \) and \( z^*_m' = 1 \), which is inconsistent with (30). In this situation, we can set \( z^*_m = 1 \) and \( z^*_m' = 0 \) to increase the objective function of Problem (sAPS-Sub) but without violating any constraint. We thus finish the proof.

Based on Proposition 5 and (30), we can express the optimal objective function value of Problem (sAPS-Sub) as follows

\[
RW^\text{sub}_{s}(\Lambda_s, n) = \sum_{m \in \Lambda_s} \left( \mu H^\text{req}_m - \pi(p^*_s, \{ |H^\text{max}_s, n| \} + p^*_B,(s), \{ |H^\text{max}_s, n| \}) \right) z^*_m,(n).
\]

(31)

2) **Solving Problem (sAPS-Top) and Problem (MultiMUSel-sAPs)**: Based on (30) and (31), we then solve Problem (sAPS-Top). Since Problem (sAPS-Top) only involves an integer variable \( n = \{ 0, 1, 2, \ldots, \min\{|\Lambda_s|, H^\text{max}_s\} \} \), we propose sAPSol-Algorithm, which is based on the enumeration of \( n \) within \( \{ 0, 1, 2, \ldots, \min\{|\Lambda_s|, H^\text{max}_s\} \} \), to find the optimal \( n^* \) that can maximize the objective function \( RW_s(\Lambda_s) \). Notice that our proposed sAPSol-Algorithm also solves Problem (MultiMUSel-sAPs) and outputs the optimal solution \( \{ z^*_m \} m \in \Lambda_s \) (as well as the corresponding \( RW_s(\Lambda_s) \)).

**E. Proposed Algorithm to Solve Problem (MultiMUSel-sAPs)**

By using sAPSol-Algorithm as the subroutine to compute \( RW_s(\Lambda_s) \) (for each sAP) under the given \( \Lambda_s \), we then continue to solve Problem (MultiMUSel-sAPs). Thanks to the simple form, Problem (MultiMUSel-sAPs) can be considered as an optimal grouping problem that assigns the MUs into the sets \( \{ \Lambda_s \} s \in \{ 0, 1 \} \). We use \( \{ \Lambda^*_s \} s \in \{ 0, 1 \} \) to denote the optimal solution of Problem (MultiMUSel-sAPs). To find \( \{ \Lambda^*_s \} s \in \{ 0, 1 \} \), we propose the following SelSol-Algorithm. The key of SelSol-Algorithm is to execute a randomized local search based on the idea of simulated annealing [39].

- In each round of iteration, a randomly selected sAP \( s \) randomly selects a MU \( j \) in \( \Lambda_s \) and moves this MU \( j \) to another randomly selected sAP \( s' \). If such a MU-switch can improve the total reward of sAP \( s \) and sAP \( s' \), then sAP \( s \) and sAP \( s' \) accept such a MU-switch by updating \( \Lambda_s = \Lambda_s \setminus \{ j \} \) and \( \Lambda_{s'} = \Lambda_{s'} \cup \{ j \} \). Please notice that for the sake of easy presentation, we introduce \( sAP 0 \) as a virtual sAP which manages \( \Lambda_0 \).
- To avoid being trapped in the local optimum, we adopt the idea of Simulated Annealing (SA) [39, 40] to accept the non-improvement MU-switch with a certain probability (in Step 4). In particular, the probability to accept
sAPSol-Algorithm: To Solve Problem (MultiMUSel-sAP) and Output \(\{s_{sm,(i)}\}_{m\in\Lambda_s}\) and \(\text{RW}_s(\Lambda_s)\)

1: Input \(\Lambda_s\) for sAP \(s\)
2: Initialize CBV = 0, CBS = œ, and \(n = 0\).
3: while \(n \leq \min\{\alpha \} \leq \text{HH}_{\text{max}}\) do
   4: sAP \(s\) uses ADLS-Algorithm to compute \((p_{s,(i)}, p_{B_1(s),(i)})\) for each MU \(i \in \Lambda_s\), and obtain \(n_{t_{\text{FB}}(i)}\).
   5: if Problem (sAP-sub) is infeasible according to (30) then
     6: sAP sets \(n = n + 1\) and starts the next round of iteration.
   7: else
     8: sAP uses (30) to compute \((s_{sm,(i)})_{m\in\Lambda_s}\) and uses (31) to compute \(\text{RW}_s^{\text{FB}}(\Lambda_s,n)\).
     9: if \(\text{RW}_s^{\text{FB}}(\Lambda_s,n) > \text{CBV}\) then
       10: sAP sets \(\text{CBV} = \text{RW}_s^{\text{FB}}(\Lambda_s,n)\), and set CBS = \(\{s_{sm,(i)}\}_{m\in\Lambda_s}\).
       11: end if
     12: sAP sets \(n = n + 1\).
     13: end if
   14: end while
15: Output: \(\text{RW}_s(\Lambda_s) = \text{CBV}\) and \(\{s_{sm,(i)}\}_{m\in\Lambda_s} = \text{CBS}\).

SelSol-Algorithm: To Solve Problem (MultiMUSel-Top) and Output \(\{\Lambda_s\}_{s\in\mathcal{S} \bigcup \{0\}}\)

1: Initialization: assign the MUs into \(\{\Lambda_s\}_{s\in\mathcal{S} \bigcup \{0\}}\) in a round-robin manner, set the iteration index \(t = 1\), and set the initial temperature \(T_{\text{ini}} = 100\).
2: Each sAP \(s\) uses sAPSol-algorithm to compute \(\text{RW}_s(\Lambda_s)\), and the virtual sAP 0 sets \(\text{RW}_0(\Lambda_0) = 0\) directly.
3: while (1) do
   4: Randomly select an sAP (let us say \(s\)) with nonempty \(\Lambda_s\), and sAP \(s\) randomly selects a MU \(j \in \Lambda_s\). sAP \(s\) further randomly selects another sAP \(s' \neq s\).
   5: sAP \(s\) moves MU \(j\) to sAP \(s'\). Correspondingly, sAP \(s\) sets \(\Lambda_s = \Lambda_s \setminus \{j\}\), and sAP \(s\) sets \(\Lambda_s' = \Lambda_s' \cup \{j\}\).
   6: if \(\text{RW}_s(\Lambda_s) + \text{RW}_s(\Lambda_s') > \text{RW}_s(\Lambda_s) + \text{RW}_s(\Lambda_s')\) then
     7: sAP \(s\) updates \(\Lambda_s = \Lambda_s\) and sAP \(s'\) updates \(\Lambda_s' = \Lambda_s'\).
   8: else
     9: With probability equal to \(\exp\{-\frac{\Delta_{\text{RT}}}{T_t}\}\) where \(\Delta = \text{RW}_s(\Lambda_s) + \text{RW}_s(\Lambda_s') - \text{RW}_s(\Lambda_s) - \text{RW}_s(\Lambda_s')\), and \(T_t = \frac{T_{\text{ini}}}{1 + x + x^t}\) is the system temperature at time \(t\), \(s\) is the Boltzmann constant. sAP \(s\) uses sAPSol-algorithm to compute \(\Lambda_s = \Lambda_s\), and sAP \(s'\) updates \(\Lambda_s' = \Lambda_s'\).
   10: end if
   11: if the set of \(\{\Lambda_s\}_{s\in\mathcal{S}}\) do not change for consecutive iterations then
     12: Reach convergence and break the WHILE-LOOP.
   13: end if
   14: Update \(t = t + 1\). 
   15: end while
16: Output \(\Lambda_s = \Lambda_s, \forall s \in \mathcal{S}\).

\[ T_t \approx \frac{T_{\text{ini}}}{1 + x + x^t} \]

the non-improvement MU-switch depends on both the reward degradation and the current temperature (i.e., \(T_t\)).

Specifically, we use the cooling schedule \(T_t = \frac{T_{\text{ini}}}{1 + x + x^t}\) (with \(T_{\text{ini}}\) denoting the initial temperature, \(\alpha > 0\) being a constant, and \(t\) denoting the iteration index) [41].

4 This cooling schedule can yield an asymptotic convergence to the global optimum solution according to [42]. Specifically, based on Theorem 1 in [42], a cooling scheme can yield an asymptotic convergence to the global optimum solution, if the following conditions are satisfied, i.e., (i) \(\lim_{t \to \infty} T(t) = 0\), and (ii) \(\sum_{\text{d} = 1}^{t_{\text{FB}}} \exp\{-\frac{\text{d}^2}{T(t)}\} = \infty\), where \(\text{d}^2\) can be regarded as the distance between the optimal solution and other ones. In particular, in our Problem (MultiMUSel-Top), the value of \(\text{d}^2\) is a finite yet fixed number. Thus, we can show that the adopted cooling schedule \(T_t = \frac{T_{\text{ini}}}{1 + x + x^t}\) fits the two aforementioned conditions, which can yield the asymptotic convergence to the global optimum solution.

The higher the temperature, the more likely to accept the non-improvement MU-switch. The probability to accept the non-improvement MU-switch decreases.

After obtaining \(\{\Lambda_s\}_{s\in\mathcal{S}\bigcup\{0\}}\), we can finally compute the optimal MU-selection solution for the original Problem (MultiMUSel) (in Section V-A), by executing sAPSol-Algorithm for each sAP under the given \(\Lambda_s^*\).

As a summary of in this section, we provide Figure 4 to illustrate the connections among our proposed algorithm, and more importantly, how they work together to find the optimal solution of Problem (MultiMUSel).

VI. NUMERICAL RESULTS

A. Numerical Results for the Single sAP Case

We first validate our analytical results and the proposed algorithms for the case of one sAP. We consider a scenario in which the mBS is located at the origin (0m, 0m), and sAP \(s\) is located at (250m, 0m). The representative MU \(i\), which forms the DC-pair with sAP \(s\) is located at (220m, 0m) (later on we will specify the value of \(N_i\), i.e., the number of the MUs served by sAP \(s\)). We set the channel power gain \(g_{Bi}\) from the mBS to from MU \(i\) according to the path-loss model, i.e., \(g_{Bi} = \lambda d_{Bi}^{-\varphi}\), in which parameter \(d_{Bi}\) denotes the distance between the mBS and MU \(i\), parameter \(\varphi\) denotes the scaling-parameter (we use \(\varphi = 2.5\)), and \(\lambda\) follows an exponential distribution with the unit mean for capturing the impact of channel fading. The channel power gain \(g_{si}\) from sAP \(s\) to MU \(i\) is generated in a similar way. With this setting, the randomly generated channel power gains are \(g_{Bi} = 6.383 \times 10^{-7}\) and \(g_{si} = 8.620 \times 10^{-5}\), which are used in the following Figures 5 to 7. In addition, we set \(p_{\text{max}} = 1W\) and \(p_{\text{max}} = 0.4W\) [37], and set the bandwidths \(W_B = 10MHz\), \(W_s = 5MHz\), and set \(n_0 = 10^{-14}W\).

1) Verification of ADLS-Algorithm: Figure 5(a) shows the operations of ADLS-Algorithm that enumerates \(\rho_{si}\) for solving Problem (OGPm). We set \(N_s = 3\). Recall that for each enumerated \(\rho_{si}\), we use SubSol-Algorithm to compute \((\hat{\tau}_{si}(\rho_{si}), \hat{p}_{si}(\rho_{si}))\), and use (13) and (14) to compute \(\hat{x}_{Bi}(\rho_{si})\) and \(\hat{p}_{Bi}(\rho_{si})\), respectively. In addition, we use (18) to compute \(\rho_{si}^{\text{FB}} = 0.6228\) (which is marked out in Figure 5(a)). The top-subplot of Figure 5(a) shows that \(\hat{\tau}_{si}(\rho_{si}), \hat{p}_{si}(\rho_{si})\) leads to the zero-outage when \(\rho_{si} \geq \rho_{si}^{\text{FB}}\), which thus validates Proposition 2. The bottom-subplot of...
Figure 5(a) shows the on-grid power consumption \( \hat{p}_{si}(\rho_{si}) + \hat{p}_{Bi}(\rho_{si}) \) when enumerating \( \rho_{si} \). Meanwhile, we use (21) to compute \( \hat{p}_{si},Z + \hat{p}_{Bi}(Z) \), which is marked out by the red circle. In particular, \( \hat{p}_{si},Z + \hat{p}_{Bi}(Z) \) exactly corresponds to the minimum of \( \hat{p}_{si}(\rho_{si}) + \hat{p}_{Bi}(\rho_{si}) \) for the interval of \( \rho_{si} \in [\rho_{si}^{\text{cri}}, 1] \). This validates our analysis for the zero-outage case and our proposed ADLS-Algorithm, i.e., directly calculating \( \rho_{si}^* + \hat{p}_{Bi}(Z) \) instead of using the linear-search for \( \rho_{si} \in [\rho_{si}^{\text{cri}}, 1] \).

2) Advantage of ADLS-Algorithm: Figure 5(b) shows the advantage of ADLS-Algorithm in reducing the iterations, in comparison with LS-Algorithm. As stated in Section IV, by using the analytical solution (21) for the zero-outage case, ADLS-Algorithm can avoid the linear-search of \( \rho_{si} \in [\rho_{si}^{\text{cri}}, 1] \), which thus reduces the number of required iterations.

Specifically, we plot the ratio of reduced iterations (i.e., the value of \( 1 - \frac{\rho_{si}^*}{\rho_{si}^{\text{cri}}} \)) by using ADLS-Algorithm in Figure 5(b).

Figure 5(b) shows that the reduced ratio increases quickly in both MU \( i \)'s traffic requirement and the number of the MUs served by sAP \( x \). This result means that our ADLS-Algorithm is more computationally efficient when the MU's traffic requirement (or the total number of the MUs served by the sAP) is larger.

3) Illustration of Optimal Offloading Solution: Figure 6(a) illustrates the optimal solution of Problem (OGPM) versus different traffic requirements. Here, we set \( N_s = 7 \) (i.e., the sAP is serving 7 MUs). The top-subplot of Figure 6(a) plots sAP \( s \)'s optimal on-grid transmit-power, the mBS's optimal transmit-power, and the minimum total on-grid power consumption. As shown in the top-subplot of Figure 6(a), when the MU's traffic requirement is low, the minimum total on-grid power consumption is zero. This is because that we can completely rely on the sAP's EH power-supply to power the offloading in order to meet the MU's traffic requirement.

However, when the MU's traffic requirement increases, the sAP's EH power-supply alone cannot satisfy the MU's requirement. Thus, the sAP needs to spend a non-zero on-grid power to afford the MU's requirement, which yields the increase in the sAP's optimal on-grid power. Moreover, when the MU's traffic requirement further increases, traffic offloading through the sAP will consume a large on-grid power. As a result, the mBS needs to spend a non-zero on-grid power to afford part of the MU's traffic requirement, which yields the increase in the mBS's optimal on-grid power consumption.

In this situation, the corresponding optimal offloading-ratio (i.e., the value of \( 1 - \frac{x_{Bi}^*/Z}{R_{\text{req}}} \)) starts to decrease, as shown in the bottom-subplot of Figure 6(a). In particular, the bottom-subplot of Figure 6(a) also shows that the successful offloading probability (i.e., the value of \( 1 - P_{\text{out}}(\rho_{si}^*, \rho_{si}^*) \)) gradually increases to one, when the MU's traffic requirement increases. As a result, the sAP needs to be more conservative in relying on the EH power supply, but using more on-grid power to support the traffic offloading. This is essentially because that a larger offloading outage probability will lead to a larger waste of the sAP's on-grid power consumption.

4) Advantage of Optimal Offloading Solution: Figure 6(b) further shows the advantage of the proposed optimal offloading scheme in reducing the total on-grid power consumption. For the purpose of comparison, we also consider another offloading scheme in which the MU offloads a fixed portion of its traffic requirement to the sAP (we set such a portion as 70%, 80%, 90%, and 100% in Figure 6(b)). The results validate the advantage of our proposed offloading scheme, i.e., it can minimize the total on-grid power consumption while guaranteeing the served MU's traffic requirement. This advantage is essentially achieved by our formulated joint optimization of the traffic scheduling and power allocation, which is able to jointly reap the benefit of DC-capability (to flexibly schedule the MU's traffic between macro and small cells) and the benefit of exploiting EH power-supply (to reduce the on-grid power consumption). In comparison, the fixed offloading scheme fails to achieve these benefits. Specifically, as shown in Figure 6(b), due to the fact the sAP's EH power-supply cannot accommodate a very large offloading rate, offloading too much of the MU's traffic (i.e., the 100%-offloading) will lead to a quick
increase in the total on-grid power consumption when the MU’s traffic requirement increases.

5) Impact of the EH Power-Supply: To evaluate the impact of the EH power-supply, we plot the optimal solution versus different degrees of the randomness of the EH power-supply in Figure 7(a). We set $N_s = 2$ and $M_s^{\text{low}} = 0.01$, and vary $M_s^{\text{upp}}$ from 0.05 to 0.25, which corresponds to a larger average EH power-supply. As shown in the top-subplot of Figure 7(a), the MU’s optimal total on-grid power consumption decreases as $M_s^{\text{upp}}$ increases. Such a decrease in the total on-grid power consumption essentially stems from that we rely more on the EH power-supply to power the MU’s traffic offloading, which yields a decrease in the successful probability of traffic delivery, as shown in the bottom-subplot of Figure 7(a).

6) Impact of the Number of the Served MUs: Due to sharing the sAP’s harvested energy, the number of the MUs served by the sAP (i.e., the value of $N_s$) will influence the optimal offloading solution of Problem (OGPM). To evaluate this impact, we plot the optimal solution versus different values of $N_s$ in Figure 7(b). As shown in the top-subplot of Figure 7(b), the optimal total on-grid power consumption increases when $N_s$ increases, which is due to the fact each MU is allocated a smaller amount of harvested energy when $N_s$ increases. Correspondingly, to satisfy the MU’s traffic requirement, sAP $s$ needs to use more on-grid power to support the traffic offloading, which consequently yields an increase in the successful probability of traffic delivery, as shown in the bottom-subplot of Figure 7(b). In particular, Figure 7(b) also indicates that we need to carefully determine the numbers of the MUs served by each sAP in the multi-sAP scenario.

B. Numerical Results for the Case of Multiple sAPs

We next evaluate our proposed algorithms for the case of multiple sAPs, and show the performance gain of the optimal MU-selection solution of Problem (MultiMUSel). We consider a scenario that the mBS is located at the origin (0m, 0m), and three sAPs are located at (212m, 10m), (220m, −8m), and (235m, 6m). The group of MUs are randomly located within the plane whose center is (220m, 0m) and radius is 20m, i.e., the MUs are geographically closer to the sAPs than the mBS (this is a favorable condition for traffic offloading).

The channel power gains and other parameters are randomly set as described before.

1) Illustration of the Optimal MU-Selection Solution: We first illustrate the optimal MU-selection solution of Problem (MultiMUSel), which is yielded by our proposed SelSol-Algorithm. Figure 8 shows the optimal MU-selection solution for two different cases. Specifically, Figure 8(a) shows the case of all sAPs with a homogeneous EH-capacity (i.e., $M_s^{\text{low}} = 0.01$ and $M_s^{\text{upp}} = 0.2$, $s = 1,2,3$). In this case, the optimal solution shows that the sAPs select different MUs to provide traffic offloading in an almost balanced way, namely, both sAP 1 and sAP 2 serve 6 MUs, and sAP 3 serves 8 MUs. Figure 8(b) shows the case of the sAPs with heterogeneous EH-capacity. To illustrate the result clearly, we set sAP 1 with $M_s^{\text{low}} = 0.01$ and $M_s^{\text{upp}} = 0.2$, and sAP 2 and sAP 3 with $M_s^{\text{low}} = 0.01$ and $M_s^{\text{upp}} = 0.4$, namely, sAP 3 has a much larger EH-power-supply than sAP 1 and sAP 2. As a result, to fully exploit the EH power-supply and reduce the total on-grid power consumption for whole network, sAP 3 selects 12 MUs to offload traffic, as shown in Figure 8(b).

2) Advantage of the Optimal MU-Selection Solution: We next show the performance advantage of our SelSol-Algorithm in Figure 9. For comparison, we also show the results of a distance-based scheme in which each MU aggressively selects the sAP with the shortest distance for traffic offloading. Similar to Figure 10(b), we use the case that the sAPs are of heterogeneous EH-capacity. Figure 9(a) shows the results under different numbers of the MUs. Specifically, we fix 4 sAPs at (212m, 10m), (220m, −8m), (235m, 6m), and (250m, −3m). We vary the number of the MUs from 16 to 30, and fix each MU’s traffic requirement as 40Mbps. In Figure 9(a), we mark out the relative improvement achieved by our proposed algorithm against the distance-based scheme on the top of each tested case. Figure 9(a) shows that the achieved average reward gradually increases as the number

Every point in Figure 9 represents the average result of 20 realizations of the MUs’ geographical distributions.
of the MUs increases, since the sAPs have a larger freedom in selecting different MUs for executing the traffic offloading. Figure 9(a) validates that the average reward can be significantly increased by using our proposed SelSol-Algorithm. As shown in Figure 9(a), our SelSol-Algorithm can improve the reward up to 58.6% in comparison with the distance-based scheme. The performance advantage not only comes from that we exploit the benefit of the DC-enabled traffic offloading which provides a flexible traffic scheduling and power allocation, but also comes from that we properly exploit the sAPs’ EH power-supply by avoiding too many MUs offloading through a same sAP.

Figure 9(b) shows the results under different traffic requirements. Specifically, we fix 4 APs and 8 MUs, and vary each

![Fig. 7. Optimal solution of Problem (OGPM) under different parameter-settings.](image)

![Fig. 8. Examples of the optimal MU-selection solution of Problem (MultiMUSel) under μ = 0.025$/Mbps and π = 0.002/KW.](image)

![Fig. 9. Performance advantage of the optimal MU-selection solution.](image)
supply, we have proposed the joint optimization of the traffic and power consumption of macro and small cells. We firstly focus on the single sAP case, and have proposed an efficient layered-algorithm to compute the optimal offloading solution for each pair of sAP-MU. We then study the multi-sAP case and investigate how different small cells select the MUs for maximizing the total network-reward. We have also proposed an efficient algorithm to compute the optimal MG solution. Extensive numerical results have been provided to validate our proposed algorithms and the performance advantages of the proposed DC-enabled traffic offloading through the EH-powered small cells.

For our future work, we will further consider that the sAP can flexibly schedule its EH power-supply over different time slots and allocate different amounts of the EH power-supply for different MUs, and investigate the optimal design of the DC-enabled traffic offloading for improving the energy-efficiency.

VII. CONCLUSION

In this paper, we have investigated the energy-efficient DC-enabled traffic offloading through the EH-powered small cells. To reap the advantages of the DC-capability and the EH power-supply, we have proposed the joint optimization of the traffic scheduling and power allocation to minimize the total on-grid power consumption of macro and small cells. We firstly focus on the single sAP case, and have proposed an efficient layered-algorithm to compute the optimal offloading solution for each pair of sAP-MU. We then study the multi-sAP case and investigate how different small cells select the MUs for maximizing the total network-reward. We have also proposed an efficient algorithm to compute the optimal MG solution. Extensive numerical results have been provided to validate our proposed algorithms and the performance advantages of the proposed DC-enabled traffic offloading through the EH-powered small cells.

For our future work, we will further consider that the sAP can flexibly schedule its EH power-supply over different time slots and allocate different amounts of the EH power-supply for different MUs, and investigate the optimal design of the DC-enabled traffic offloading for improving the energy-efficiency.

REFERENCES


less heterogeneous network framework for 5G systems,” IEEE Commun.
Mag., vol. 52, no. 5, pp. 94–101, May 2014.
green mobile networking: From the perspectives of network opera-
tors and mobile users,” IEEE Commun. Surveys Tuts., vol. 17, no. 3,
p. 1515–1556, 3rd Quart, 2015.
cell cooperation,” IEEE Wireless Commun., vol. 20, no. 1, pp. 82–89,
oriented traffic offloading in wireless networks: A brief survey and a
small-cell operation,” IEEE J. Sel. Areas Commun., vol. 34, no. 5,
and energy efficiency of heterogeneous wireless networks with intra-
inter-RAT offloading,” IEEE Trans. Veh. Technol., vol. 64, no. 7,
trade-off for green small cell networks,” in Proc. IEEE ICC, London,
resource allocation for multi-RAT heterogeneous networks,” IEEE J.
turned off via vertical offloading under a separation architecture?” IEEE
aware cooperative traffic offloading via device-to-device cooperations:
An analytical approach,” IEEE Trans. Mobile Comput., vol. 16, no. 1,
management via real-time electricity price control in smart grids,” IEEE
May 2016.
[22] T. Han and N. Ansari, “ICE: Intelligent cell breathing to optimize
the utilization of green energy,” IEEE Commun. Lett., vol. 16, no. 6,
[23] T. Han and N. Ansari, “Green-energy aware and latency aware
user associations in heterogeneous cellular networks,” in Proc. IEEE
GLOBECOM Workshops, Atlanta, GA, USA, 2013, pp. 4946–4951.
energy powered base station connected to a microgrid,” in Proc. IEEE
GLOBECOM, Austin, TX, USA, 2014, pp. 2721–2726.
allocation and data offloading for energy efficiency in wireless power
transfer enabled collaborative mobile clouds,” in Proc. IEEE INFOCOM
Workshops, Hong Kong, 2015, pp. 336–341.
and resource allocation in renewable energy powered cellular networks,”
[27] T. Han, J. Lee, T. Q. S. Quek, and Y.-W. P. Hong, “Traffic offloading in
heterogeneous networks with energy harvesting personal-cell networks
relay placement and sub-carrier allocation in wireless communication
fading wireless link with energy harvesting transmitter and receiver,”
outage probability minimization with an energy harvesting transmitter,”
[33] A. Mehrabi and K. Kim, “General framework for network throughput
maximization in sink-based energy harvesting wireless sensor networks,”
Recharge Time in a Stochastic Energy Harvesting System. [Online].
[37] National Instruments. Introduction to UMTS Device Testing Transmitter
Introduction_to_UMTS_Device_Testing.pdf
[38] J. B. Mazzola and A. W. Neebe, “Resource-constrained assignment
simulated annealing,” in Encyclopedia of Artificial Intelligence. Hershey,
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